

# FOCUS ACADEMY

Kg to 12

English&Gujarati Medium

BRANCH 1- 19-B MUSLIM SOC, B/H  
FIRDOS MASJID DANILIMDA  
AHMEDABAD

BRANCH2-2<sup>ND</sup> 3<sup>RD</sup> AND 4<sup>TH</sup>  
FLOOR, UNIQUE APT. JUHAPURA  
CROSS ROAD, AHMEDABAD

## Class 9 Maths Chapter 12 Heron's Formula

### Ex 12.1

A traffic signal board, indicating 'SCHOOL AHEAD', is an equilateral triangle with side  $a$ . Find the area of the signal board, using Heron's formula. If its perimeter is 180 cm, what will be the area of the signal board?

**Solution:**

Let each side of the equilateral triangle be  $a$ .

Semi-perimeter of the triangle,

$$s = \frac{a+a+a}{2} = \frac{3a}{2}$$

$$\text{Area of the triangle} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{s(s-a)(s-a)(s-a)} = \sqrt{s(s-a)^3}$$

$$= \sqrt{\frac{3a}{2} \left(\frac{3a}{2} - a\right)^3}$$

$$= \sqrt{\frac{3a}{2} \times \left(\frac{a}{2}\right)^3}$$

$$= \sqrt{\frac{3a^4}{2^4}} = \frac{\sqrt{3}}{4} a^2$$



Now, its perimeter is 180 cm.

$$\therefore a + a + a = 180 \text{ cm}$$

$$\Rightarrow 3a = 180 \text{ cm}$$

$$\Rightarrow a = \frac{180}{3} \text{ cm} = 60 \text{ cm}$$

$$\text{Thus, area of the triangle} = \frac{\sqrt{3}}{4} a^2$$

$$= \frac{\sqrt{3}}{4} (60)^2 \text{ cm}^2$$

$$= 900\sqrt{3} \text{ cm}^2$$

### Question 2.

The triangular side walls of a flyover have been used for advertisements. The sides of the walls are 122 m, 22 m and 120 m (see figure). The advertisements yield an earning of ₹5000

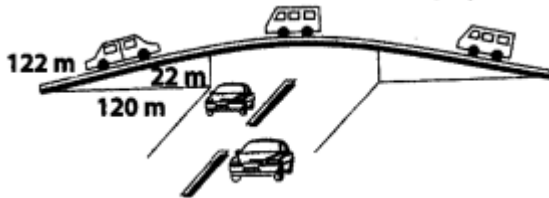
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per m<sup>2</sup> per year. A company hired one of its walls for 3 months. How much rent did it pay?



**Solution:**

Let the sides of the triangular wall be

$$a = 122\text{m}, b = 120\text{m}, c = 22\text{m}$$

Semi-perimeter,  $s = \frac{a+b+c}{2}$

$$\left(\frac{122+120+22}{2}\right)\text{m} = 132\text{m}$$

The area of the triangular side wall

$$= \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{132(132-122)(132-120)(132-22)} \text{ m}^2$$

$$= \sqrt{132 \times 10 \times 12 \times 110} \text{ m}^2$$

$$= \sqrt{12 \times 11 \times 10 \times 12 \times 11 \times 10} \text{ m}^2 = 1320 \text{ m}^2$$

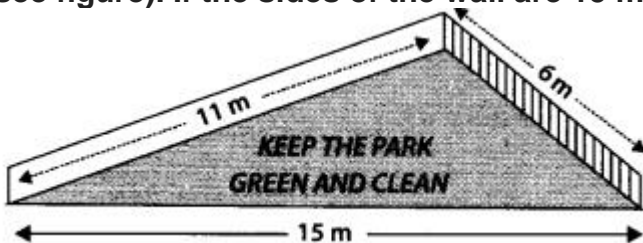
Rent for 1 year (i.e. 12 months) per m<sup>2</sup> = Rs. 5000

∴ Rent for 3 months per m<sup>2</sup> = Rs. 5000 ×  $\frac{3}{12}$

= Rent for 3 months for 1320 m<sup>2</sup> = Rs. 5000 ×  $\frac{3}{12}$  × 1320 = Rs. 16,50,000.

**Question 3.**

There is a slide in a park. One of its side walls has been painted in some colour with a message “KEEP THE PARK GREEN AND CLEAN” (see figure). If the sides of the wall are 15 m, 11 m and 6m, find the area painted in colour.



**Solution:**

Let the sides of the wall be

$$a = 15\text{m}, b = 11\text{m}, c = 6\text{m}$$

Semi-perimeter,

$$s = \frac{a+b+c}{2} = \left(\frac{15+11+6}{2}\right)\text{m} = \frac{32}{2}\text{m} = 16\text{m}$$

Now, area of the triangular surface of the wall

$$= \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{16(16-15)(16-11)(16-6)} \text{ m}^2$$

$$= \sqrt{16 \times 1 \times 5 \times 10} \text{ m}^2$$

$$= \sqrt{2 \times 400} \text{ m}^2 = 20\sqrt{2} \text{ m}^2$$

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Thus, the required area painted in colour  
=  $20\sqrt{2} \text{ m}^2$

**Question 4.**

Find the area of a triangle two sides of which are 18 cm and 10 cm and the perimeter is 42 cm.

**Solution:**

Let the sides of the triangle be  $a = 18 \text{ cm}$ ,  $b = 10 \text{ cm}$  and  $c = x \text{ cm}$

Since, perimeter of the triangle = 42 cm

$$\therefore 18\text{cm} + 10 \text{ cm} + x\text{cm} = 42$$

$$x = [42 - (18 + 10)\text{cm}] = 14\text{cm}$$

Now, semi-perimeter,  $s = \frac{42\text{cm}}{2} = 21 \text{ cm}$

$$\text{Area of the triangle} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{21(21-18)(21-10)(21-14)} \text{ cm}^2$$

$$= \sqrt{21 \times 3 \times 11 \times 7} \text{ cm}^2$$

$$= \sqrt{3 \times 7 \times 3 \times 11 \times 7} \text{ cm}^2 = 21\sqrt{11} \text{ cm}^2$$

Thus, the required area of the triangle =  $21\sqrt{11} \text{ cm}^2$

**Question 5.**

Sides of a triangle are in the ratio of 12 : 17 : 25 and its perimeter is 540 cm. Find its area.

**Solution:**

Let the sides of the triangle be

$$a = 12x \text{ cm}, b = 17x \text{ cm}, c = 25x \text{ cm}$$

Perimeter of the triangle = 540 cm

$$\text{Now, } 12x + 17x + 25x = 540$$

$$\Rightarrow 54x = 540 \Rightarrow x = 10$$

$$\therefore a = (12 \times 10)\text{cm} = 120\text{cm},$$

$$b = (17 \times 10) \text{ cm} = 170 \text{ cm}$$

$$\text{and } c = (25 \times 10)\text{cm} = 250 \text{ cm}$$

Now, semi-perimeter,  $s = \frac{540\text{cm}}{2} = 270 \text{ cm}$

$$\text{Area of the triangle} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{270(270-120)(270-170)(270-250)} \text{ cm}^2$$

$$= \sqrt{270 \times 150 \times 100 \times 20} \text{ cm}^2$$

$$= \sqrt{10^2 \times 10^2 \times 3^2 \times 3^2 \times 5^2 \times 2^2} \text{ cm}^2$$

$$= (10 \times 10 \times 3 \times 3 \times 5 \times 2) \text{ cm}^2 = 9,000 \text{ cm}^2$$

**Question 6.**

An isosceles triangle has perimeter 30 cm and each of the equal sides is 12 cm. Find the area of the triangle.

**Solution:**

Let the sides of an isosceles triangle be

$$a = 12\text{cm}, b = 12\text{cm}, c = x \text{ cm}$$

Since, perimeter of the triangle = 30 cm

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$$\therefore 12\text{cm} + 12\text{cm} + x\text{ cm} = 30\text{ cm}$$

$$\Rightarrow x = (30 - 24) = 6$$

Now, semi-perimeter,  $s = \frac{30}{2} = 15\text{ cm}$

$$\therefore \text{Area of the triangle} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{15(15-12)(15-12)(15-6)}\text{ cm}^2$$

$$= \sqrt{15 \times 3 \times 3 \times 9}\text{ cm}^2$$

$$= \sqrt{5 \times 3 \times 3 \times 3 \times 3 \times 3}\text{ cm}^2$$

$$= \sqrt{3^2 \times 3^2 \times 3 \times 5}\text{ cm}^2$$

$$= 3 \times 3 \times \sqrt{3 \times 5}\text{ cm}^2 = 9\sqrt{15}\text{ cm}^2$$

Thus, the required area of the triangle =  $9\sqrt{15}\text{ cm}^2$

## Ex 12.2

**Ex 12.2 Class 9 Maths Question 1.**

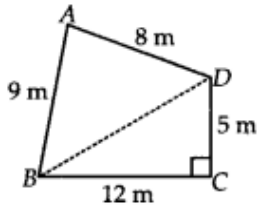
A park, in the shape of a quadrilateral ABCD, has  $\angle C = 90^\circ$ ,  $AB = 9\text{m}$ ,  $BC = 12\text{m}$ ,  $CD = 5\text{m}$  and  $AD = 8\text{ m}$ .

How much area does it occupy?

**Solution:**

Given, a quadrilateral ABCD with  $\angle C = 90^\circ$ ,  $AB = 9\text{ m}$ ,  $BC = 12\text{ m}$ ,  $CD = 5\text{ m}$  and  $AD = 8\text{ m}$ .

Let us join B and D, such that ABCD is a right angled triangle.



$$\begin{aligned} \text{We have, area of } \triangle BCD &= \frac{1}{2} \times BC \times CD \\ &= \left( \frac{1}{2} \times 12 \times 5 \right) \text{ m}^2 \\ &= 30 \text{ m}^2 \end{aligned}$$

Now, to find the area of  $\triangle ABD$ , we need the length of BD.

In right-angled  $\triangle BCD$ , by Pythagoras theorem

$$BD^2 = BC^2 + CD^2$$

$$\Rightarrow BD^2 = 12^2 + 5^2$$

$$\Rightarrow BD^2 = 144 + 25 = 169$$

$$\Rightarrow BD = 13\text{ m}$$

Now, for  $\triangle ABD$ , we have

$$a = AB = 9\text{ m}, b = AD = 8\text{ m}, c = BD = 13\text{ m}$$

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$$\text{Semi-perimeter, } s = \frac{a+b+c}{2}$$

$$= \left( \frac{9+8+13}{2} \right) \text{m} = \frac{30}{2} \text{m} = 15 \text{m}$$

$$\text{Area of } \triangle ABD = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{15(15-9)(15-8)(15-13)} \text{ m}^2$$

$$= \sqrt{15 \times 6 \times 7 \times 2} \text{ m}^2$$

$$= \sqrt{3 \times 5 \times 3 \times 2 \times 7 \times 2} \text{ m}^2$$

$$= \sqrt{3^2 \times 2^2 \times 5 \times 7} \text{ m}^2 = 3 \times 2\sqrt{35} \text{ m}^2$$

$$= 6 \times 5.916 \text{ m}^2 = 35.5 \text{ m}^2 \text{ (approx.)}$$

$$\therefore \text{Area of quadrilateral ABCD} = \text{area of } \triangle BCD + \text{area of } \triangle ABD = 30 \text{ m}^2 + 35.5 \text{ m}^2$$

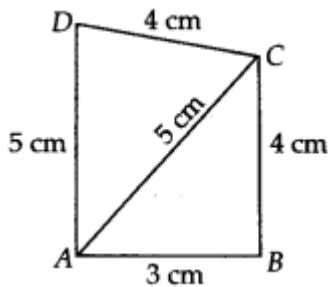
$$= 65.5 \text{ m}^2 \text{ (approx.)}$$

### Ex 12.2 Class 9 Maths Question 2.

Find the area of a quadrilateral ABCD in which AB = 3 cm, BC = 4 cm, CD = 4 cm, DA = 5 cm and AC = 5 cm.

**Solution:**

Given a quadrilateral ABCD with AB = 3 cm, BC = 4 cm, CD = 4 cm, DA = 5 cm and AC = 5 cm.



For  $\triangle ABC$ ,  $a = AB = 3 \text{ cm}$ ,  $b = BC = 4 \text{ cm}$  and  $c = AC = 5 \text{ cm}$

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$$\text{Semi-perimeter, } s = \frac{a + b + c}{2}$$

$$= \left( \frac{3 + 4 + 5}{2} \right) \text{ cm} = 6 \text{ cm}$$

$$\text{Area of } \Delta ABC = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{6(6-3)(6-4)(6-5)} \text{ cm}^2$$

$$= \sqrt{6 \times 3 \times 2 \times 1} \text{ cm}^2$$

$$= \sqrt{3 \times 2 \times 3 \times 2} \text{ cm}^2 = 6 \text{ cm}^2$$

For  $\Delta ACD$ ,  $a = AD = 5 \text{ cm}$ ,  $b = CD = 4 \text{ cm}$  and  $c = AC = 5 \text{ cm}$

$$\text{Semi-perimeter, } s = \frac{a + b + c}{2}$$

$$= \left( \frac{5 + 4 + 5}{2} \right) \text{ cm} = \frac{14}{2} \text{ cm} = 7 \text{ cm}$$

$$\text{Area of } \Delta ACD = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{7(7-5)(7-4)(7-5)} \text{ cm}^2$$

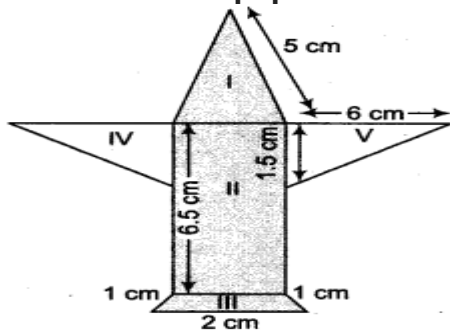
$$= \sqrt{7 \times 2 \times 3 \times 2} \text{ cm}^2 = 2\sqrt{21} \text{ cm}^2$$

$$= 2 \times 4.6 \text{ cm}^2 = 9.2 \text{ cm}^2 \text{ (approx.)}$$

Now, area of quadrilateral ABCD = area of  $\Delta ABC$  + area of  $\Delta ACD$   
 $= 6 \text{ cm}^2 + 9.2 \text{ cm}^2 = 15.2 \text{ cm}^2$  (approx.)

### Question 3.

Radha made a picture of an aeroplane with coloured paper as shown in figure. Find the total area of the paper used.



**Solution:**

For surface I:

It is an isosceles triangle whose sides are  $a = 5 \text{ cm}$ ,  $b = 5 \text{ cm}$ ,  $c = 6 \text{ cm}$

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$$s = \frac{a+b+c}{2} = \left(\frac{5+5+1}{2}\right) \text{cm} = \frac{11}{2} \text{cm}$$

$$\text{Area of surface I} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{\frac{11}{2} \left(\frac{11}{2} - 5\right) \left(\frac{11}{2} - 5\right) \left(\frac{11}{2} - 1\right)} \text{cm}^2$$

$$= \sqrt{\frac{11}{2} \times \frac{1}{2} \times \frac{1}{2} \times \frac{9}{2}} \text{cm}^2 = \frac{3}{4} \sqrt{11} \text{cm}^2$$

$$= (0.75 \times 3.3) \text{cm}^2$$

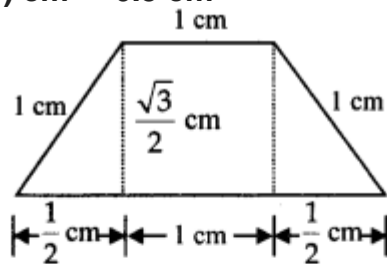
$$= 2.475 \text{cm}^2 \text{ (approx.)}$$

**For surface II:**

It is a rectangle with length 6.5 cm and breadth 1 cm.

∴ Area of surface II = Length x Breadth

$$= (6.5 \times 1) \text{cm}^2 = 6.5 \text{cm}^2$$



Its height is given by

$$h = \sqrt{1^2 - \left(\frac{1}{2}\right)^2} \text{cm} = \sqrt{1 - \frac{1}{4}} \text{cm}$$

$$= \sqrt{\frac{3}{4}} \text{cm} = \frac{\sqrt{3}}{2} \text{cm}$$

Area of a trapezium

$$= \frac{1}{2} [(\text{Sum of the parallel sides}) \times \text{Height}]$$

∴ Area of surface III

$$= \frac{1}{2} \times \left[ (2+1) \times \frac{\sqrt{3}}{2} \right] \text{cm}^2$$

$$= \frac{3\sqrt{3}}{4} \text{cm}^2 = \frac{3 \times 1.732}{4} \text{cm}^2 \text{ (approx.)}$$

$$= 1.3 \text{cm}^2 \text{ (approx.)}$$

**For surface III:**

It is a trapezium whose parallel sides are 1 cm and 2 cm as shown in the figure given

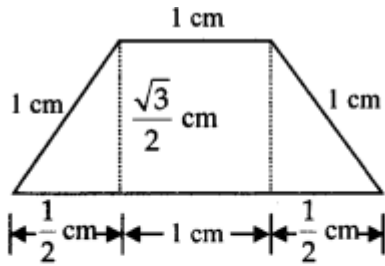
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below:



Its height is given by

$$h = \sqrt{1^2 - \left(\frac{1}{2}\right)^2} \text{ cm} = \sqrt{1 - \frac{1}{4}} \text{ cm}$$
$$= \sqrt{\frac{3}{4}} \text{ cm} = \frac{\sqrt{3}}{2} \text{ cm}$$

Area of a trapezium

$$= \frac{1}{2} [(\text{Sum of the parallel sides}) \times \text{Height}]$$

$\therefore$  Area of surface III

$$= \frac{1}{2} \times \left[ (2 + 1) \times \frac{\sqrt{3}}{2} \right] \text{ cm}^2$$
$$= \frac{3\sqrt{3}}{4} \text{ cm}^2 = \frac{3 \times 1.732}{4} \text{ cm}^2 (\text{approx.})$$
$$= 1.3 \text{ cm}^2 (\text{approx.})$$

For surface IV and V:

Surface V is a right-angled triangle with base 6 cm and height 1.5 cm.

Also, area of surface IV = area of surface V

= 1/2 x base x height

$$= (1/2 \times 6 \times 1.5) \text{ cm}^2 = 4.5 \text{ cm}^2$$

Thus, the total area of the paper used = (area of surface I) + (area of surface II) + (area of surface III) + (area of surface IV) + (area of surface V) = [2.475 + 6.5 + 1.3 + 4.5 + 4.5] cm<sup>2</sup>

$$= 19.275 \text{ cm}^2$$

$$= 19.3 \text{ cm}^2 (\text{approx.})$$

Question 4.

A triangle and a parallelogram have the same base and the same area. If the sides of the triangle are 26 cm, 28 cm and 30 cm, and the parallelogram stands on the base 28 cm, find the height of the parallelogram

Solution:

For the given triangle, we have a = 28 cm, b = 30 cm, c = 26 cm

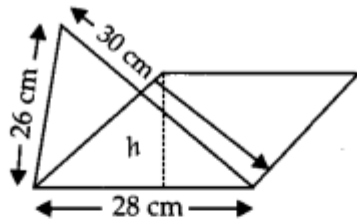
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$$\text{Semi-perimeter, } s = \frac{a + b + c}{2}$$

$$= \left( \frac{28 + 30 + 26}{2} \right) \text{ cm}$$

$$= \frac{84}{2} \text{ cm} = 42 \text{ cm}$$

$$\text{Area of the triangle} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{42(42-28)(42-30)(42-26)} \text{ cm}^2$$

$$= \sqrt{42 \times 14 \times 12 \times 16} \text{ cm}^2$$

$$= \sqrt{112896} \text{ cm}^2 = 336 \text{ cm}^2$$

Area of the given parallelogram = Area of the given triangle

∴ Area of the parallelogram =  $336 \text{ cm}^2$

⇒ base x height = 336

⇒  $28 \times h = 336$ , where 'h' be the height of the parallelogram.

⇒  $h = \frac{336}{28} = 12$

Thus, the required height of the parallelogram = 12 cm

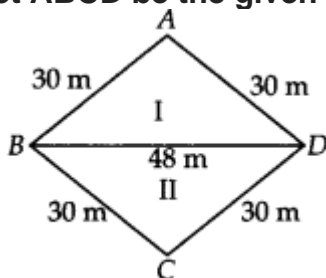
Ex 12.2 Class 9 Maths Question 5.

A rhombus shaped field has green grass for 18 cows to graze. If each side of the rhombus is 30 m and its longer diagonal is 48 m, how much area of grass field will each cow be getting?

Solution:

Here, each side of the rhombus = 30 m.

Let ABCD be the given rhombus and the diagonal,  $BD = 48 \text{ m}$



Sides  $\triangle ABC$  are  $a = AB = 30 \text{ m}$ ,  $b = AD = 30 \text{ m}$ ,  $c = BD = 48 \text{ m}$

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$$\text{Semi-perimeter, } s = \frac{a + b + c}{2}$$

$$= \left( \frac{30 + 30 + 48}{2} \right) \text{ m}$$

$$= \frac{108}{2} \text{ m} = 54 \text{ m}$$

$$\text{Area of triangle I} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{54(54-30)(54-30)(54-48)} \text{ m}^2$$

$$= \sqrt{54 \times 24 \times 24 \times 6} \text{ m}^2 = \sqrt{186624} \text{ m}^2$$

$$= 432 \text{ m}^2$$

Since, a diagonal divides the rhombus into two congruent triangles.

∴ Area of triangle II = 432 m<sup>2</sup>

Now, total area of the rhombus = Area of triangle I + Area of triangle II

$$= 432 \text{ m}^2 + 432 \text{ m}^2 = 864 \text{ m}^2$$

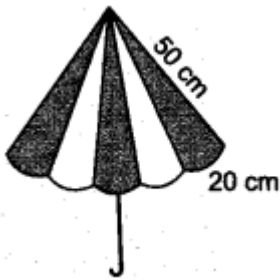
Area of grass for 18 cows to graze = 864 m<sup>2</sup>

⇒ Area of grass for 1 cow to graze = 864/18 m<sup>2</sup>

$$= 48 \text{ m}^2$$

Ex 12.2 Class 9 Maths Question 6.

An umbrella is made by stitching 10 triangular pieces of cloth of two different colours (see figure), each piece measuring 20 cm, 50 cm and 50 cm. How much cloth of each colour is required for the umbrella?



**Solution:**

Let the sides of each triangular piece be

$$a = 20 \text{ cm, } b = 50 \text{ cm, } c = 50 \text{ cm}$$

$$\text{Semi-perimeter, } s = \frac{a + b + c}{2}$$

$$= \left( \frac{20 + 50 + 50}{2} \right) \text{ cm}$$

$$= \frac{120}{2} \text{ cm} = 60 \text{ cm}$$

Area of each triangular piece

$$= \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{60(60-20)(60-50)(60-50)} \text{ cm}^2$$

$$= \sqrt{60 \times 40 \times 10 \times 10} \text{ cm}^2 = 200\sqrt{6} \text{ cm}^2$$

Area of 5 triangular pieces of one colour

$$= 5 \times 200\sqrt{6} \text{ cm}^2 = 1000\sqrt{6} \text{ cm}^2$$

∴ Area of 5 triangular pieces of other colour

$$= 1000\sqrt{6} \text{ cm}^2$$

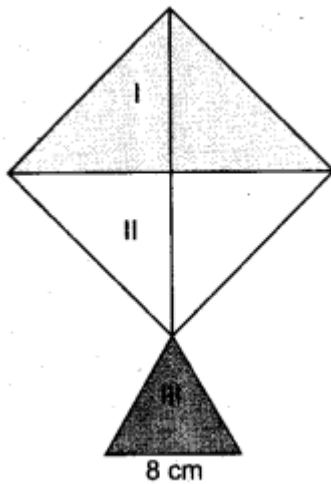
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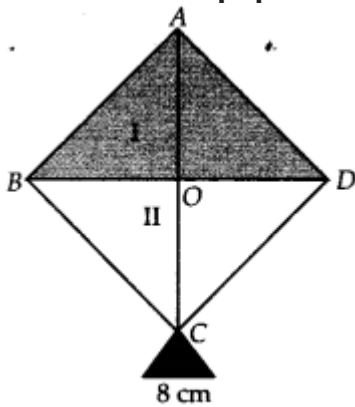
**Question 7.**

A kite in the shape of a square with a diagonal 32 cm and an isosceles triangle of base 8 cm and sides 6 cm each is to be made of three different shades as shown in figure. How much paper of each shade has been used in it?



**Solution:**

Each shade of paper is divided into 3 triangles i.e., I, II, III



8 cm

For triangle I:

ABCD is a square [Given]

∴ Diagonals of a square are equal and bisect each other.

∴ AC = BD = 32 cm

Height of AABD = OA =  $(\frac{1}{2} \times 32)$  cm

= 16 cm

Area of triangle I =  $(\frac{1}{2} \times 32 \times 16)$  cm<sup>2</sup>

= 256 cm<sup>2</sup>

For triangle II:

Since, diagonal of a square divides it into two congruent triangles.

So, area of triangle II = area of triangle I

∴ Area of triangle II = 256 cm<sup>2</sup>

For triangle III:

The sides are given as a = 8 cm, b = 6 cm and c = 6 cm

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$$\text{Semi-perimeter, } s = \frac{a+b+c}{2}$$

$$= \left( \frac{8+6+6}{2} \right) \text{ cm} = 10 \text{ cm}$$

$$\text{Area of triangle III} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{10(10-8)(10-6)(10-6)} \text{ cm}^2$$

$$= \sqrt{10 \times 2 \times 4 \times 4} \text{ cm}^2$$

$$= \sqrt{2 \times 5 \times 2 \times 4 \times 4} \text{ cm}^2$$

$$= 8\sqrt{5} \text{ cm}^2 = 8 \times 2.24 \text{ cm}^2$$

$$= 17.92 \text{ cm}^2 \text{ (approx.)}$$

Thus, the area of different shades are:

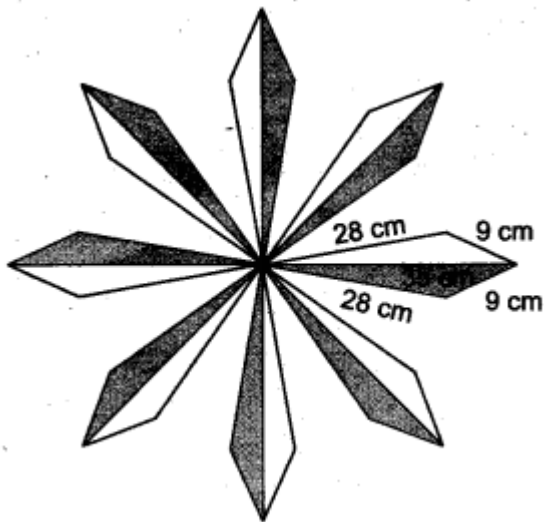
Area of shade I = 256 cm<sup>2</sup>

Area of shade II = 256 cm<sup>2</sup>

and area of shade III = 17.92 cm<sup>2</sup>

**Question 8.**

A floral design on a floor is made up of 16 tiles which are triangular, the sides of the triangle being 9 cm, 28 cm and 35 cm (see figure). Find the cost of polishing the tiles at the rate of 50 paise per cm<sup>2</sup>.



**Solution:**

Let the sides of the triangle be  $a = 9 \text{ cm}$ ,  $b = 28 \text{ cm}$ ,  $c = 35 \text{ cm}$

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$$\text{Semi-perimeter, } s = \frac{a + b + c}{2}$$

$$= \left( \frac{9 + 28 + 35}{2} \right) \text{cm}$$

$$= \frac{72}{2} \text{cm} = 36 \text{cm}$$

$$\text{Area of the triangle} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{36(36-9)(36-28)(36-35)} \text{ cm}^2$$

$$= \sqrt{36 \times 27 \times 8 \times 1} \text{ cm}^2$$

$$= 3 \times 2 \times 3 \times 2\sqrt{3 \times 2} \text{ cm}^2$$

$$= 36\sqrt{6} \text{ cm}^2 = (36 \times 2.45) \text{ cm}^2$$

$$= 88.2 \text{ cm}^2 \text{ (approx.)}$$

Total area of all the 16 triangles =  $(16 \times 88.2) \text{ cm}^2 = 1411.2 \text{ cm}^2$  (approx.)

Cost of polishing the tiles = Rs. 0.5 per  $\text{cm}^2$

$\therefore$  Cost of polishing all the tiles = Rs.  $(0.5 \times 1411.2) = \text{Rs. } 705.60$  (approx.)

### Question 9.

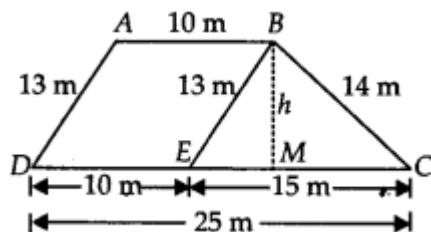
A field is in the shape of a trapezium whose parallel sides are 25 m and 10 m. The non-parallel sides are 14 m and 13 m. Find the area of the field.

Solution:

Let the given field is in the form of a trapezium ABCD such that parallel sides are AB = 10 m and DC = 25 m

Non-parallel sides are AD = 13 m and BC = 14 m.

We draw BE || AD, such that BE = 13 m.



The given field is divided into two shapes (i)  $\triangle BCE$ , (ii) parallelogram ABED For  $\triangle BCE$ :

Sides of the triangle are  $a = 13 \text{ m}$ ,  $b = 14 \text{ m}$ ,  $c = 15 \text{ m}$

$$\text{Semi-perimeter, } s = \frac{a + b + c}{2}$$

$$= \left( \frac{13 + 14 + 15}{2} \right) \text{m} = \frac{42}{2} \text{m} = 21 \text{m}$$

$$\text{Area of } \triangle BCE = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{21(21-13)(21-14)(21-15)} \text{ m}^2$$

$$= \sqrt{21 \times 8 \times 7 \times 6} \text{ m}^2 = \sqrt{7056} \text{ m}^2 = 84 \text{ m}^2$$

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**(ii) For parallelogram ABED:**

**Let the height of the  $\triangle BCE$  corresponding to the side EC be h m.**

**Area of a triangle =  $\frac{1}{2} \times \text{base} \times \text{height}$**

$$\therefore \frac{1}{2} \times 15 \times h = 84$$

$$\Rightarrow (10 + 82) \times 15 = 565$$

**Now, area of a parallelogram = base  $\times$  height**

$$= (10 \times 565) = (2 \times 56) \text{ m}^2 = 112 \text{ m}^2$$

**So, area of the field**

$$= \text{area of } \triangle BCE + \text{area of parallelogram ABED}$$

$$= 84 \text{ m}^2 + 112 \text{ m}^2 = 196 \text{ m}^2$$

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