

“Known For Best Result”

FOCUS

Class 9

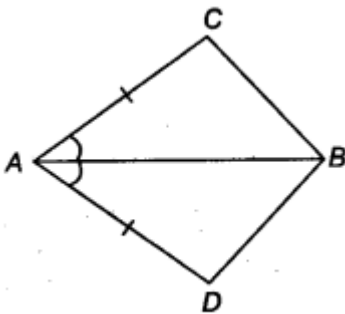
Maths

Chapter 7 Triangles

Ex 7.1

Ex 7.1 Class 9 Maths Question 1.

In quadrilateral ACBD, $AC = AD$ and AB bisects $\angle A$ (see figure). Show that $\triangle ABC \cong \triangle ABD$. What can you say about BC and BD ?



Solution:

In quadrilateral ACBD, we have $AC = AD$ and AB being the bisector of $\angle A$.

Now, In $\triangle ABC$ and $\triangle ABD$,

$AC = AD$ (Given)

$\angle CAB = \angle DAB$ (AB bisects $\angle CAB$)

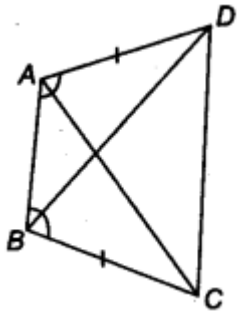
and $AB = AB$ (Common)

$\therefore \triangle ABC \cong \triangle ABD$ (By SAS congruence axiom)

$\therefore BC = BD$ (By CPCT)

Question 2.

ABCD is a quadrilateral in which $AD = BC$ and $\angle DAB = \angle CBA$ (see figure). Prove that



- (i) $\triangle ABD \cong \triangle BAC$
(ii) $BD = AC$
(iii) $\angle ABD = \angle BAC$

Solution:

In quadrilateral ACBD, we have $AD = BC$ and $\angle DAB = \angle CBA$

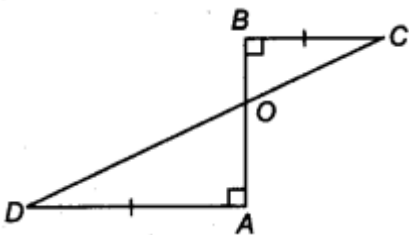
- (i) In $\triangle ABD$ and $\triangle BAC$,
 $AD = BC$ (Given)
 $\angle DAB = \angle CBA$ (Given)
 $AB = AB$ (Common)
 $\therefore \triangle ABD \cong \triangle BAC$ (By SAS congruence)

- (ii) Since $\triangle ABD \cong \triangle BAC$
 $\Rightarrow BD = AC$ [By C.P.C.T.]

- (iii) Since $\triangle ABD \cong \triangle BAC$
 $\Rightarrow \angle ABD = \angle BAC$ [By C.P.C.T.]

Ex 7.1 Class 9 Maths Question 3.

AD and BC are equal perpendiculars to a line segment AB (see figure). Show that CD bisects AB.



Solution:

In $\triangle BOC$ and $\triangle AOD$, we have

$$\angle BOC = \angle AOD$$

$$BC = AD \text{ [Given]}$$

$$\angle BOC = \angle AOD \text{ [Vertically opposite angles]}$$

$$\therefore \triangle OBC \cong \triangle OAD \text{ [By AAS congruency]}$$

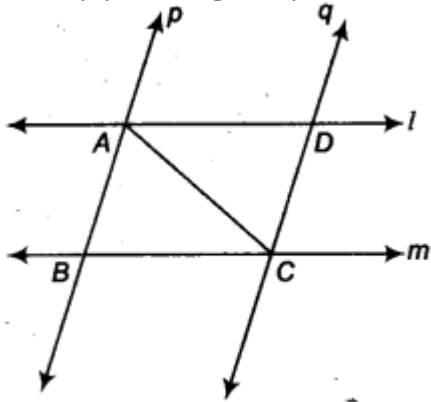
$$\Rightarrow OB = OA \text{ [By C.P.C.T.]}$$

i.e., O is the mid-point of AB.

Thus, CD bisects AB.

Ex 7.1 Class 9 Maths Question 4.

l and m are two parallel lines intersected by another pair of parallel lines p and q (see figure). Show that $\triangle ABC = \triangle CDA$.



Solution:

$\because p \parallel q$ and AC is a transversal,

$\therefore \angle BAC = \angle DCA \dots(1)$ [Alternate interior angles]

Also $l \parallel m$ and AC is a transversal,

$\therefore \angle BCA = \angle DAC \dots(2)$

[Alternate interior angles]

Now, in $\triangle ABC$ and $\triangle CDA$, we have

$\angle BAC = \angle DCA$ [From (1)]

$CA = AC$ [Common]

$\angle BCA = \angle DAC$ [From (2)]

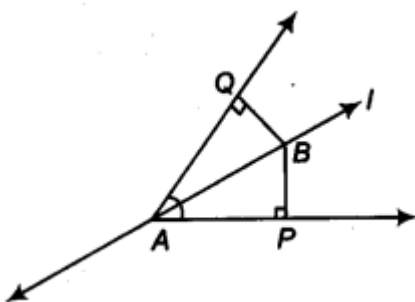
$\therefore \triangle ABC \cong \triangle CDA$ [By ASA congruency]

Ex 7.1 Class 9 Maths Question 5.

Line l is the bisector of an $\angle A$ and $\angle B$ is any point on l. BP and BQ are perpendiculars from B to the arms of LA (see figure). Show that

(i) $\triangle APB \cong \triangle AQB$

(ii) $BP = BQ$ or B is equidistant from the arms of $\angle A$.



Solution:

We have, l is the bisector of $\angle QAP$.

$\therefore \angle QAB = \angle PAB$

$\angle Q = \angle P$ [Each 90°]

$\angle ABQ = \angle ABP$

[By angle sum property of A]

Now, in $\triangle APB$ and $\triangle AQB$, we have

$\angle ABP = \angle ABQ$ [Proved above]

$AB = BA$ [Common]

$\angle PAB = \angle QAB$ [Given]

$\therefore \triangle APB \cong \triangle AQB$ [By ASA congruency]

Since $\triangle APB \cong \triangle AQB$

$\Rightarrow BP = BQ$ [By C.P.C.T.]

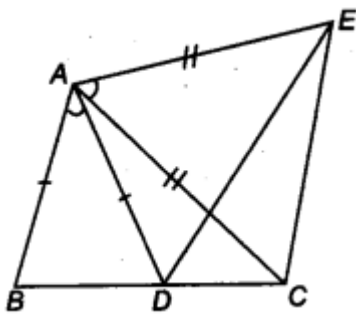
i. e., [Perpendicular distance of B from AP]

= [Perpendicular distance of B from AQ]

Thus, the point B is equidistant from the arms of $\angle A$.

Ex 7.1 Class 9 Maths Question 6.

In figure, $AC = AE$, $AB = AD$ and $\angle BAD = \angle EAC$. Show that $BC = DE$.



Solution:

We have, $\angle BAD = \angle EAC$

Adding $\angle DAC$ on both sides, we have

$\angle BAD + \angle DAC = \angle EAC + \angle DAC$

$\Rightarrow \angle BAC = \angle DAE$

Now, in $\triangle ABC$ and $\triangle ADE$. we have

$\angle BAC = \angle DAE$ [Proved above]

$AB = AD$ [Given]

$AC = AE$ [Given]

$\therefore \triangle ABC \cong \triangle ADE$ [By SAS congruency]

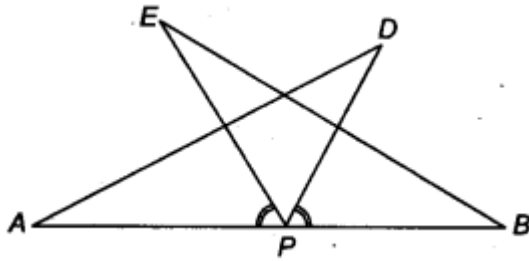
$\Rightarrow BC = DE$ [By C.P.C.T.]

Ex 7.1 Class 9 Maths Question 7.

AS is a line segment and P is its mid-point. D and E are points on the same side of AB such that $\angle BAD = \angle ABE$ and $\angle EPA = \angle DPB$. (see figure). Show that

(i) $\triangle DAP \cong \triangle EBP$

(ii) $AD = BE$



Solution:

We have, P is the mid-point of AB.

$$\therefore AP = BP$$

$$\angle EPA = \angle DPB \text{ [Given]}$$

Adding $\angle EPD$ on both sides, we get

$$\angle EPA + \angle EPD = \angle DPB + \angle EPD$$

$$\Rightarrow \angle APD = \angle BPE$$

(i) Now, in $\triangle DAP$ and $\triangle EBP$, we have

$$\angle PAD = \angle PBE \text{ [} \because \angle BAD = \angle ABE \text{]}$$

$$AP = BP \text{ [Proved above]}$$

$$\angle DPA = \angle EPB \text{ [Proved above]}$$

$$\therefore \triangle DAP \cong \triangle EBP \text{ [By ASA congruency]}$$

(ii) Since, $\triangle DAP \cong \triangle EBP$

$$\Rightarrow AD = BE \text{ [By C.P.C.T.]}$$

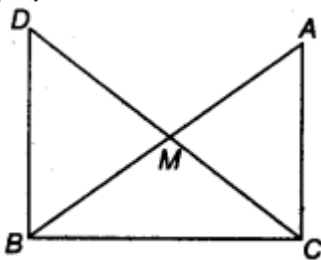
Ex 7.1 Class 9 Maths Question 8.

In right triangle ABC, right angled at C, M is the mid-point of hypotenuse AB. C is joined to M and produced to a point D such that $DM = CM$. Point D is joined to point B (see figure). Show that

$$(i) \triangle AMC \cong \triangle BMD$$

$$(ii) \angle DBC \text{ is a right angle}$$

$$(iii) \triangle DBC \cong \triangle ACB$$



$$(iv) CM = \frac{1}{2} AB$$

Solution:

Since M is the mid – point of AB.

$$\therefore BM = AM$$

(i) In $\triangle AMC$ and $\triangle BMD$, we have

$$CM = DM \text{ [Given]}$$

Focus Academy Ahmedabad

8780038581, 9099818013, 8780997670

www.focusacademyahmedabad.com

$\angle AMC = \angle BMD$ [Vertically opposite angles]

$AM = BM$ [Proved above]

$\therefore \triangle AMC \cong \triangle BMD$ [By SAS congruency]

(ii) Since $\triangle AMC \cong \triangle BMD$

$\Rightarrow \angle MAC = \angle MBD$ [By C.P.C.T.]

But they form a pair of alternate interior angles.

$\therefore AC \parallel DB$

Now, BC is a transversal which intersects parallel lines AC and DB,

$\therefore \angle BCA + \angle DBC = 180^\circ$ [Co-interior angles]

But $\angle BCA = 90^\circ$ [$\triangle ABC$ is right angled at C]

$\therefore 90^\circ + \angle DBC = 180^\circ$

$\Rightarrow \angle DBC = 90^\circ$

(iii) Again, $\triangle AMC \cong \triangle BMD$ [Proved above]

$\therefore AC = BD$ [By C.P.C.T.]

Now, in $\triangle DBC$ and $\triangle ACB$, we have

$BD = CA$ [Proved above]

$\angle DBC = \angle ACB$ [Each 90°]

$BC = CB$ [Common]

$\therefore \triangle DBC \cong \triangle ACB$ [By SAS congruency]

(iv) As $\triangle DBC \cong \triangle ACB$

$DC = AB$ [By C.P.C.T.]

But $DM = CM$ [Given]

$\therefore CM = 12DC = 12AB$

$\Rightarrow CM = 12AB$

Ex 7.2 Class 9 Maths Question 1.

In an isosceles triangle ABC, with $AB = AC$, the bisectors of $\angle B$ and $\angle C$ intersect each other at O. Join A to O. Show that

(i) $OB = OC$

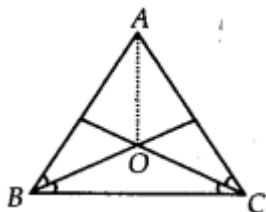
(ii) AO bisects $\angle A$

Solution:

i) in $\triangle ABC$, we have

$AB = AC$ [Given]

$\therefore \angle ABC = \angle ACB$ [Angles opposite to equal sides of a \triangle are equal]



$\Rightarrow 12\angle ABC = 12\angle ACB$

or $\angle OBC = \angle OCB$

$\Rightarrow OC = OB$ [Sides opposite to equal angles of a Δ are equal]

(ii) In ΔABO and ΔACO , we have

$AB = AC$ [Given]

$\angle OBA = \angle OCA$ [$\because \angle B = \angle C$]

$OB = OC$ [Proved above]

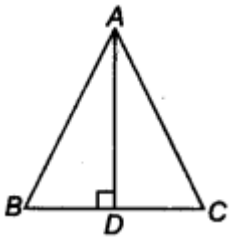
$\Delta ABO \cong \Delta ACO$ [By SAS congruency]

$\Rightarrow \angle OAB = \angle OAC$ [By C.P.C.T.]

$\Rightarrow AO$ bisects $\angle A$.

Ex 7.2 Class 9 Maths Question 2.

In ΔABC , AD is the perpendicular bisector of BC (see figure). Show that ΔABC is an isosceles triangle in which $AB = AC$.



Solution:

Since AD is bisector of BC .

$\therefore BD = CD$

Now, in ΔABD and ΔACD , we have

$AD = DA$ [Common]

$\angle ADB = \angle ADC$ [Each 90°]

$BD = CD$ [Proved above]

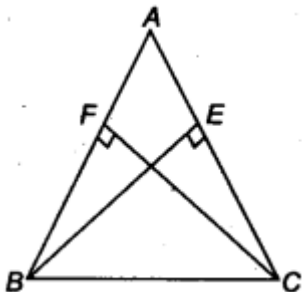
$\therefore \Delta ABD \cong \Delta ACD$ [By SAS congruency]

$\Rightarrow AB = AC$ [By C.P.C.T.]

Thus, ΔABC is an isosceles triangle.

Ex 7.2 Class 9 Maths Question 3.

ABC is an isosceles triangle in which altitudes BE and CF are drawn to equal sides AC and AB respectively (see figure). Show that these altitudes are equal.



Solution:

ΔABC is an isosceles triangle.

$\therefore AB = AC$

$\Rightarrow \angle ACB = \angle ABC$ [Angles opposite to equal sides of a Δ are equal]

$\Rightarrow \angle BCE = \angle CBF$

Now, in ΔBEC and ΔCFB

$\angle BCE = \angle CBF$ [Proved above]

$\angle BEC = \angle CFB$ [Each 90°]

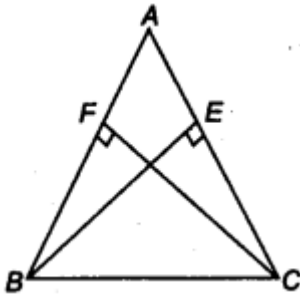
$BC = CB$ [Common]

$\therefore \Delta BEC \cong \Delta CFB$ [By AAS congruency]

So, $BE = CF$ [By C.P.C.T.]

Ex 7.2 Class 9 Maths Question 4.

ABC is a triangle in which altitudes BE and CF to sides AC and AB are equal (see figure).



Show that

(i) $\Delta ABE \cong \Delta ACF$

(ii) $AB = AC$ i.e., ABC is an isosceles triangle.

Solution:

(i) In ΔABE and ΔACF , we have

$\angle AEB = \angle AFC$

[Each 90° as $BE \perp AC$ and $CF \perp AB$]

$\angle A = \angle A$ [Common]

$BE = CF$ [Given]

$\therefore \Delta ABE \cong \Delta ACF$ [By AAS congruency]

(ii) Since, $\Delta ABE \cong \Delta ACF$

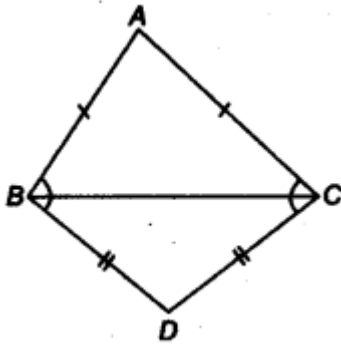
$\therefore AB = AC$ [By C.P.C.T.]

$\Rightarrow ABC$ is an isosceles triangle.

Ex 7.2 Class 9 Maths Question 5.

ABC and DBC are isosceles triangles on the same base BC (see figure).

Show that $\angle ABD = \angle ACD$.



Solution:

In $\triangle ABC$, we have

$AB = AC$ [$\triangle ABC$ is an isosceles triangle]

$\therefore \angle ABC = \angle ACB \dots(1)$

[Angles opposite to equal sides of a \triangle are equal]

Again, in $\triangle BDC$, we have

$BD = CD$ [$\triangle BDC$ is an isosceles triangle]

$\therefore \angle CBD = \angle BCD \dots(2)$

[Angles opposite to equal sides of a \triangle are equal]

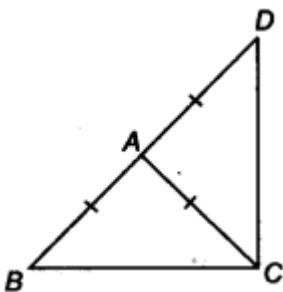
Adding (1) and (2), we have

$\angle ABC + \angle CBD = \angle ACB + \angle BCD$

$\Rightarrow \angle ABD = \angle ACD.$

Ex 7.2 Class 9 Maths Question 6.

$\triangle ABC$ is an isosceles triangle in which $AB = AC$. Side BA is produced to D such that $AD = AB$ (see figure). Show that $\angle BCD$ is a right angle.



Solution:

$AB = AC$ [Given] $\dots(1)$

$AB = AD$ [Given] $\dots(2)$

From (1) and (2), we have

$AC = AD$

Now, in $\triangle ABC$, we have

$\angle ABC + \angle ACB + \angle BAC = 180^\circ$ [Angle sum property of a \triangle]

$\Rightarrow 2\angle ACB + \angle BAC = 180^\circ \dots(3)$

[$\angle ABC = \angle ACB$ (Angles opposite to equal sides of a \triangle are equal)]

Similarly, in $\triangle ACD$,

$\angle ADC + \angle ACD + \angle CAD = 180^\circ$

$\Rightarrow 2\angle ACD + \angle CAD = 180^\circ \dots(4)$

$[\angle ADC = \angle ACD$ (Angles opposite to equal sides of a Δ are equal)]

Adding (3) and (4), we have

$$2\angle ACB + \angle BAC + 2\angle ACD + \angle CAD = 180^\circ + 180^\circ$$

$$\Rightarrow 2[\angle ACB + \angle ACD] + [\angle BAC + \angle CAD] = 360^\circ$$

$$\Rightarrow 2\angle BCD + 180^\circ = 360^\circ \quad [\angle BAC \text{ and } \angle CAD \text{ form a linear pair}]$$

$$\Rightarrow 2\angle BCD = 360^\circ - 180^\circ = 180^\circ$$

$$\Rightarrow \angle BCD = 180^\circ \div 2 = 90^\circ$$

Thus, $\angle BCD = 90^\circ$

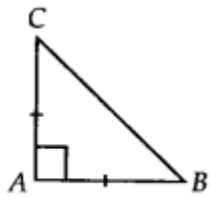
Ex 7.2 Class 9 Maths Question 7.

ΔABC is a right angled triangle in which $\angle A = 90^\circ$ and $AB = AC$, find $\angle B$ and $\angle C$.

Solution:

In ΔABC , we have $AB = AC$ [Given]

\therefore Their opposite angles are equal.



$$\Rightarrow \angle ACB = \angle ABC$$

Now, $\angle A + \angle B + \angle C = 180^\circ$ [Angle sum property of a Δ]

$$\Rightarrow 90^\circ + \angle B + \angle C = 180^\circ \quad [\angle A = 90^\circ \text{ (Given)}]$$

$$\Rightarrow \angle B + \angle C = 180^\circ - 90^\circ = 90^\circ$$

But $\angle B = \angle C$

$$\angle B = \angle C = 90^\circ \div 2 = 45^\circ$$

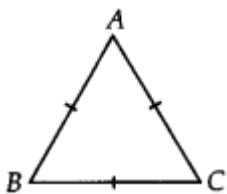
Thus, $\angle B = 45^\circ$ and $\angle C = 45^\circ$

Ex 7.2 Class 9 Maths Question 8.

Show that the angles of an equilateral triangle are 60° each.

Solution:

In ΔABC , we have



$$AB = BC = CA$$

[ΔABC is an equilateral triangle]

$$AB = BC$$

$$\Rightarrow \angle A = \angle C \dots (1) \quad [\text{Angles opposite to equal sides of a } \Delta \text{ are equal}]$$

Similarly, $AC = BC$

$$\Rightarrow \angle A = \angle B \dots (2)$$

From (1) and (2), we have

$$\angle A = \angle B = \angle C = x \text{ (say)}$$

Since, $\angle A + \angle B + \angle C = 180^\circ$ [Angle sum property of a Δ]

$$\therefore x + x + x = 180^\circ$$

$$\Rightarrow 3x = 180^\circ$$

$$\Rightarrow x = 60^\circ$$

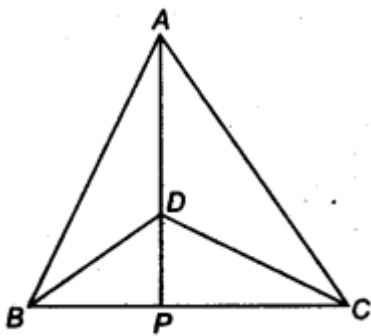
$$\therefore \angle A = \angle B = \angle C = 60^\circ$$

Thus, the angles of an equilateral triangle are 60° each.

NCERT Solutions for Class 9 Maths Chapter 7 Triangles Ex 7.3

Ex 7.3 Class 9 Maths Question 1.

$\triangle ABC$ and $\triangle DBC$ are two isosceles triangles on the same base BC and vertices A and D are on the same side of BC (see figure). If AD is extended to intersect BC at P , show that



(i) $\triangle ABD \cong \triangle ACD$

(ii) $\triangle ABP \cong \triangle ACP$

(iii) AP bisects $\angle A$ as well as $\angle D$

(iv) AP is the perpendicular bisector of BC .

Solution:

(i) In $\triangle ABD$ and $\triangle ACD$, we have

$$AB = AC \text{ [Given]}$$

$$AD = DA \text{ [Common]}$$

$$BD = CD \text{ [Given]}$$

$$\therefore \triangle ABD \cong \triangle ACD \text{ [By SSS congruency]}$$

$$\angle BAD = \angle CAD \text{ [By C.P.C.T.] ... (1)}$$

(ii) In $\triangle ABP$ and $\triangle ACP$, we have

$$AB = AC \text{ [Given]}$$

$$\angle BAP = \angle CAP \text{ [From (1)]}$$

$$\therefore AP = PA \text{ [Common]}$$

$$\therefore \triangle ABP \cong \triangle ACP \text{ [By SAS congruency]}$$

(iii) Since, $\triangle ABP \cong \triangle ACP$

$$\Rightarrow \angle BAP = \angle CAP \text{ [By C.P.C.T.]}$$

$\therefore AP$ is the bisector of $\angle A$.

Again, in $\triangle BDP$ and $\triangle CDP$,
we have $BD = CD$ [Given]

$DP = PD$ [Common]
 $BP = CP$ [$\because \triangle ABP \cong \triangle ACP$]
 $\Rightarrow \triangle BDP = \triangle CDP$ [By SSS congruency]
 $\therefore \angle BDP = \angle CDP$ [By C.P.C.T.]
 $\Rightarrow DP$ (or AP) is the bisector of $\angle BDC$
 $\therefore AP$ is the bisector of $\angle A$ as well as $\angle D$.

(iv) As, $\triangle ABP \cong \triangle ACP$
 $\Rightarrow \angle APB = \angle APC$, $BP = CP$ [By C.P.C.T.]
 But $\angle APB + \angle APC = 180^\circ$ [Linear Pair]
 $\therefore \angle APB = \angle APC = 90^\circ$
 $\Rightarrow AP \perp BC$, also $BP = CP$
 Hence, AP is the perpendicular bisector of BC .

Ex 7.3 Class 9 Maths Question 2.

AD is an altitude of an isosceles triangle ABC in which $AB = AC$. Show that

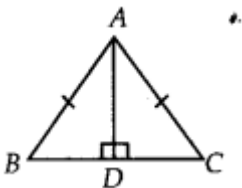
(i) AD bisects BC

(ii) AD bisects $\angle A$

Solution:

(i) In right $\triangle ABD$ and $\triangle ACD$, we have

$AB = AC$ [Given]



$\angle ADB = \angle ADC$ [Each 90°]

$AD = DA$ [Common]

$\therefore \triangle ABD \cong \triangle ACD$ [By RHS congruency]

So, $BD = CD$ [By C.P.C.T.]

$\Rightarrow D$ is the mid-point of BC or AD bisects BC .

(ii) Since, $\triangle ABD \cong \triangle ACD$,

$\Rightarrow \angle BAD = \angle CAD$ [By C.P.C.T.]

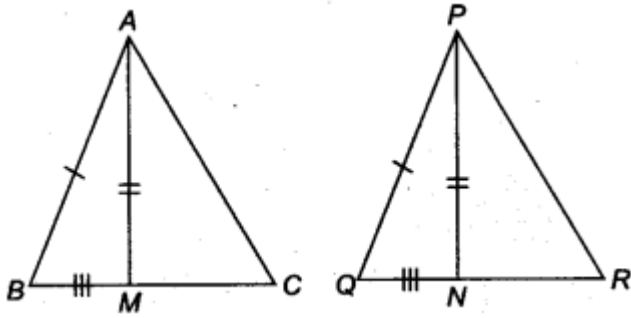
So, AD bisects $\angle A$

Ex 7.3 Class 9 Maths Question 3.

Two sides AB and BC and median AM of one triangle ABC are respectively equal to sides PQ and OR and median PN of $\triangle PQR$ (see figure). Show that

(i) $\triangle ABC \cong \triangle PQR$

(ii) $\triangle ABM \cong \triangle PQN$



Solution:

In $\triangle ABC$, AM is the median.

$$\therefore BM = \frac{1}{2} BC \dots\dots(1)$$

In $\triangle PQR$, PN is the median.

$$\therefore QN = \frac{1}{2} QR \dots(2)$$

And $BC = QR$ [Given]

$$\Rightarrow \frac{1}{2} BC = \frac{1}{2} QR$$

$$\Rightarrow BM = QN \dots(3) \text{ [From (1) and (2)]}$$

(i) In $\triangle ABM$ and $\triangle PQN$, we have

$$AB = PQ, \text{ [Given]}$$

$$AM = PN \text{ [Given]}$$

$$BM = QN \text{ [From (3)]}$$

$$\therefore \triangle ABM \cong \triangle PQN \text{ [By SSS congruency]}$$

(ii) Since $\triangle ABM \cong \triangle PQN$

$$\Rightarrow \angle B = \angle Q \dots(4) \text{ [By C.P.C.T.]}$$

Now, in $\triangle ABC$ and $\triangle PQR$, we have

$$\angle B = \angle Q \text{ [From (4)]}$$

$$AB = PQ \text{ [Given]}$$

$$BC = QR \text{ [Given]}$$

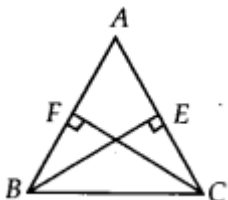
$$\therefore \triangle ABC \cong \triangle PQR \text{ [By SAS congruency]}$$

Ex 7.3 Class 9 Maths Question 4.

BE and CF are two equal altitudes of a triangle ABC. Using RHS congruence rule, prove that the triangle ABC is isosceles.

Solution:

Since $BE \perp AC$ [Given]



$\therefore BEC$ is a right triangle such that $\angle BEC = 90^\circ$

Similarly, $\angle CFB = 90^\circ$

Now, in right $\triangle BEC$ and $\triangle CFB$, we have

$$BE = CF \text{ [Given]}$$

Focus Academy Ahmedabad

8780038581, 9099818013, 8780997670

www.focusacademyahmedabad.com

$BC = CB$ [Common hypotenuse]

$\angle BEC = \angle CFB$ [Each 90°]

$\therefore \triangle BEC \cong \triangle CFB$ [By RHS congruency]

So, $\angle BCE = \angle CBF$ [By C.P.C.T.]

or $\angle BCA = \angle CBA$

Now, in $\triangle ABC$, $\angle BCA = \angle CBA$

$\Rightarrow AB = AC$ [Sides opposite to equal angles of a \triangle are equal]

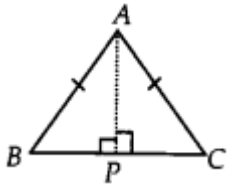
$\therefore ABC$ is an isosceles triangle.

Ex 7.3 Class 9 Maths Question 5.

ABC is an isosceles triangle with $AB = AC$. Draw $AP \perp BC$ to show that $\angle B = \angle C$.

Solution:

We have, $AP \perp BC$ [Given]



$\angle APB = 90^\circ$ and $\angle APC = 90^\circ$

In $\triangle ABP$ and $\triangle ACP$, we have

$\angle APB = \angle APC$ [Each 90°]

$AB = AC$ [Given]

$AP = AP$ [Common]

$\therefore \triangle ABP \cong \triangle ACP$ [By RHS congruency]

So, $\angle B = \angle C$ [By C.P.C.T.]

NCERT Solutions for Class 9 Maths Chapter 7 Triangles Ex 7.4

Ex 7.4 Class 9 Maths Question 1.

Show that in a right angled triangle, the hypotenuse is the longest side.

Solution:

Let us consider $\triangle ABC$ such that $\angle B = 90^\circ$

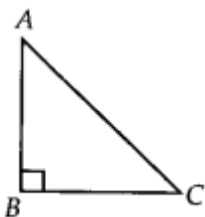
$\therefore \angle A + \angle B + \angle C = 180^\circ$

$\Rightarrow \angle A + 90^\circ + \angle C = 180^\circ$

$\Rightarrow \angle A + \angle C = 90^\circ$

$\Rightarrow \angle A + \angle C = \angle B$

$\therefore \angle B > \angle A$ and $\angle B > \angle C$



\Rightarrow Side opposite to $\angle B$ is longer than the side opposite to $\angle A$

Focus Academy Ahmedabad

8780038581, 9099818013, 8780997670

www.focusacademyahmedabad.com

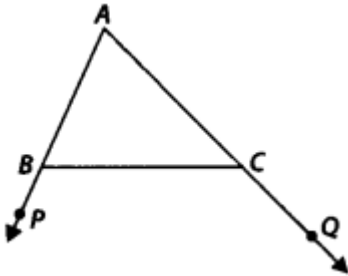
i.e., $AC > BC$.

Similarly, $AC > AB$.

Therefore, we get AC is the longest side. But AC is the hypotenuse of the triangle. Thus, the hypotenuse is the longest side.

Ex 7.4 Class 9 Maths Question 2.

In figure, sides AB and AC of $\triangle ABC$ are extended to points P and Q respectively. Also, $\angle PBC < \angle QCB$. Show that $AC > AB$.



Solution:

$\angle ABC + \angle PBC = 180^\circ$ [Linear pair]

and $\angle ACB + \angle QCB = 180^\circ$ [Linear pair]

But $\angle PBC < \angle QCB$ [Given] $\Rightarrow 180^\circ - \angle PBC > 180^\circ - \angle QCB$

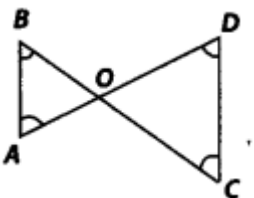
$\Rightarrow \angle ABC > \angle ACB$

The side opposite to $\angle ABC >$ the side opposite to $\angle ACB$

$\Rightarrow AC > AB$.

Ex 7.4 Class 9 Maths Question 3.

In figure, $\angle B < \angle A$ and $\angle C < \angle D$. Show that $AD < BC$.



Solution: Since $\angle A > \angle B$ [Given]

$\therefore OB > OA$... (1)

[Side opposite to greater angle is longer]

Similarly, $OC > OD$... (2)

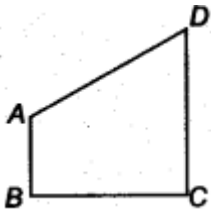
Adding (1) and (2), we have

$OB + OC > OA + OD$

$\Rightarrow BC > AD$

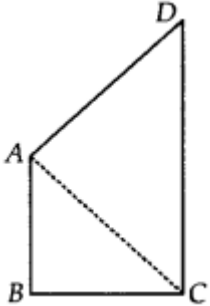
Ex 7.4 Class 9 Maths Question 4.

AB and CD are respectively the smallest and longest sides of a quadrilateral $ABCD$ (see figure). Show that $\angle A > \angle C$ and $\angle B > \angle D$.



Solution:

Let us join AC.



Now, in $\triangle ABC$, $AB < BC$ [\because AB is the smallest side of the quadrilateral ABCD]

$\Rightarrow BC > AB$

$\Rightarrow \angle BAC > \angle BCA \dots(1)$

[Angle opposite to longer side of \triangle is greater]

Again, in $\triangle ACD$, $CD > AD$

[CD is the longest side of the quadrilateral ABCD]

$\Rightarrow \angle CAD > \angle ACD \dots(2)$

[Angle opposite to longer side of \triangle is greater]

Adding (1) and (2), we get

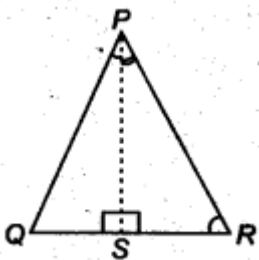
$\angle BAC + \angle CAD > \angle BCA + \angle ACD$

$\Rightarrow \angle A > \angle C$

Similarly, by joining BD, we have $\angle B > \angle D$.

Ex 7.4 Class 9 Maths Question 5.

In figure, $PR > PQ$ and PS bisect $\angle QPR$. Prove that $\angle PSR > \angle PSQ$.



Solution:

In $\triangle PQR$, PS bisects $\angle QPR$ [Given]

$\therefore \angle QPS = \angle RPS$

and $PR > PQ$ [Given]

$\Rightarrow \angle PQS > \angle PRS$ [Angle opposite to longer side of \triangle is greater]

$\Rightarrow \angle PQS + \angle QPS > \angle PRS + \angle RPS \dots(1)$ [$\because \angle QPS = \angle RPS$]

\therefore Exterior $\angle PSR = [\angle PQS + \angle QPS]$

and exterior $\angle PSQ = [\angle PRS + \angle RPS]$

Focus Academy Ahmedabad

8780038581, 9099818013, 8780997670

www.focusacademyahmedabad.com

[An exterior angle is equal to the sum of interior opposite angles]

Now, from (1), we have

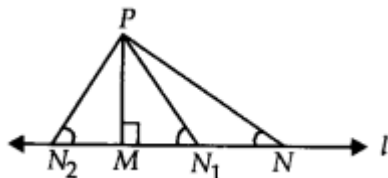
$$\angle PSR = \angle PSQ.$$

Ex 7.4 Class 9 Maths Question 6.

Show that of all line segments drawn from a given point not on it, the perpendicular line segment is the shortest.

Solution:

Let us consider the $\triangle PMN$ such that $\angle M = 90^\circ$



Since, $\angle M + \angle N + \angle P = 180^\circ$

[Sum of angles of a triangle is 180°]

$$\therefore \angle M = 90^\circ \text{ [PM} \perp \text{l]}$$

$$\text{So, } \angle N + \angle P = \angle M$$

$$\Rightarrow \angle N < \angle M$$

$$\Rightarrow \text{PM} < \text{PN} \dots(1)$$

$$\text{Similarly, } \text{PM} < \text{PN}_1 \dots(2)$$

$$\text{and } \text{PM} < \text{PN}_2 \dots(3)$$

From (1), (2) and (3), we have PM is the smallest line segment drawn from P on the line l. Thus, the perpendicular line segment is the shortest line segment drawn on a line from a point not on it.

NCERT Solutions for Class 9 Maths Chapter 7 Triangles Ex 7.5

Ex 7.5 Class 9 Maths Question 1.

ABC is a triangle. Locate a point in the interior of $\triangle ABC$ which is equidistant from all the vertices of $\triangle ABC$.

Solution:

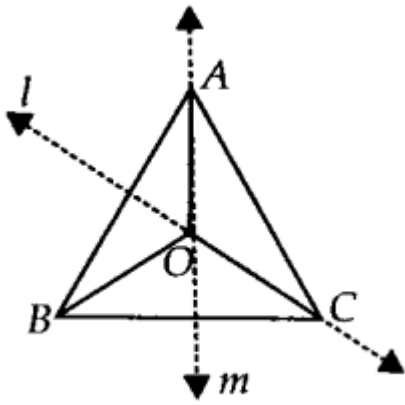
Let us consider a $\triangle ABC$.

Draw l, the perpendicular bisector of AB.

Draw m, the perpendicular bisector of BC.

Let the two perpendicular bisectors l and m meet at O.

O is the required point which is equidistant from A, B and C.



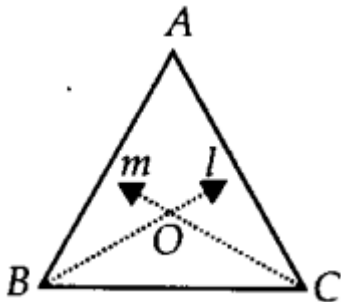
Note: If we draw a circle with centre O and radius OB or OC, then it will pass through A, B and C. The point O is called circumcentre of the triangle.

Ex 7.5 Class 9 Maths Question 2.

In a triangle locate a point in its interior which is equidistant from all the sides of the triangle.

Solution:

Let us consider a $\triangle ABC$.

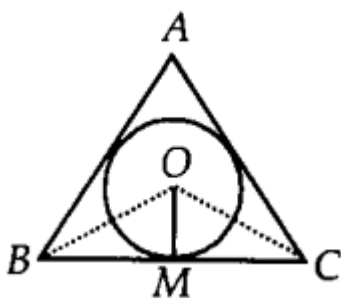


Draw m, the bisector of $\angle C$.

Let the two bisectors l and m meet at O.

Thus, O is the required point which is equidistant from the sides of $\triangle ABC$.

Note: If we draw $OM \perp BC$ and draw a circle with O as centre and OM as radius, then the circle will touch the sides of the triangle. Point O is called incentre of the triangle.



Ex 7.5 Class 9 Maths Question 3.

In a huge park, people are concentrated at three points (see figure)

A

B

C

A: where these are different slides and swings for children.

B: near which a man-made lake is situated.

C: which is near to a large parking and exist.

Where should an ice-cream parlor be set? up so that maximum number of persons can approach it?

[Hint The parlour should be equidistant from A, B and C.]

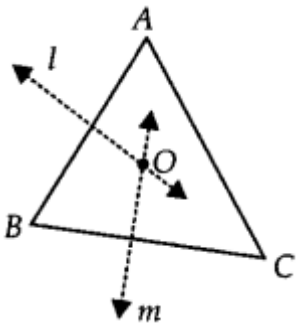
Solution:

Let us join A and B, and draw l , the perpendicular bisector of AB.

Now, join B and C, and draw m , the perpendicular bisector of BC. Let the perpendicular bisectors l and m meet at O.

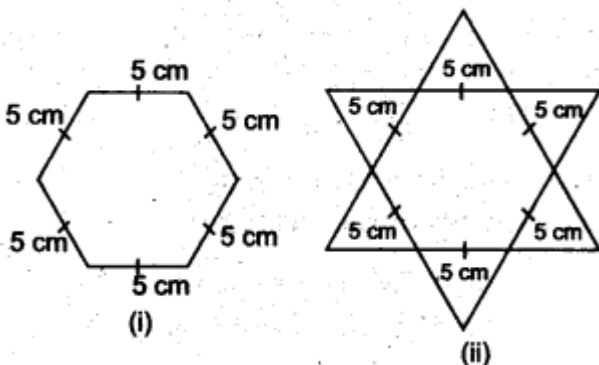
The point O is the required point where the ice cream parlour be set up.

Note: If we join A and C and draw the perpendicular bisector, then it will also meet (or pass through) the point O.



Ex 7.5 Class 9 Maths Question 4.

Complete the hexagonal and star shaped Rangolies [see Fig. (i) and (ii)] by filling them with as many equilateral triangles of side 1 cm as you can. Count the number of triangles in each case. Which has more triangles?



Solution:

It is an activity.

We require 150 equilateral triangles of side 1 cm in the Fig. (i) and 300

Focus Academy Ahmedabad

8780038581, 9099818013, 8780997670

www.focusacademyahmedabad.com

equilateral triangles in the Fig. (ii).
∴ The Fig. (ii) has more triangles.